

DEFINITION OF COMPLEX FUNCTIONS AND CALCULATION OF THEIR DERIVATIVES USING SIMPLE METHODS

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1⁰. Two function yid index , difference , multiplication and of the ratio derivative . let's say $f(x)$ and $g(x)$ functions $(a, b) \subset R$ given in being $x_0 \in (a, b)$ at the point $f'(x_0)$ and $g'(x_0)$ to derivatives have let it be Derivative to the definition according to

$$\lim_{x \rightarrow x_0} \frac{f(x) - f(x_0)}{x - x_0} = f'(x_0), (1)$$

$$\lim_{x \rightarrow x_0} \frac{g(x) - g(x_0)}{x - x_0} = g'(x_0) \quad (2)$$

will be

1) $f(x) \pm g(x)$ function x_0 at the point to the derivative have being _

$$(f(x) \pm g(x))'_{x_0} = f'(x_0) \pm g'(x_0)$$

will be

◀ $F(x) = f(x) \pm g(x)$ that we find :

$$\frac{F(x) - F(x_0)}{x - x_0} = \frac{f(x) - f(x_0)}{x - x_0} \pm \frac{g(x) - g(x_0)}{x - x_0}.$$

This in equality $x \rightarrow x_0$ at to the limit passing , relations (1) and (2) above e`attention if we can , then

$$\lim_{x \rightarrow x_0} \frac{F(x) - F(x_0)}{x - x_0} = \lim_{x \rightarrow x_0} \frac{f(x) - f(x_0)}{x - x_0} \pm$$

$$\pm \lim_{x \rightarrow x_0} \frac{g(x) - g(x_0)}{x - x_0} = f'(x_0) \pm g'(x_0)$$

to be come comes out So ,

$$F'(x_0) = (f(x) \pm g(x))'_{x_0} = f'(x_0) \pm g'(x_0). \blacktriangleright$$

2) $f(x) \cdot g(x)$ function x_0 at the point to the derivative have being _

$$(f(x) \cdot g(x))'_{x_0} = f'(x_0) \cdot g(x_0) \pm f(x_0) \cdot g'(x_0)$$

will be

◀ $\Phi(x) = f(x) \cdot g(x)$ that

$$\frac{\Phi(x) - \Phi(x_0)}{x - x_0}$$

ratio as follows

$$\frac{\Phi(x) - \Phi(x_0)}{x - x_0} = \frac{f(x) - f(x_0)}{x - x_0} \cdot g(x_0) + \frac{g(x) - g(x_0)}{x - x_0} \cdot f(x)$$

writing we can After $x \rightarrow x_0$ to the limit at past we find :

$$\begin{aligned} \lim_{x \rightarrow x_0} \frac{\Phi(x) - \Phi(x_0)}{x - x_0} &= g(x_0) \cdot \lim_{x \rightarrow x_0} \frac{f(x) - f(x_0)}{x - x_0} + \lim_{x \rightarrow x_0} \frac{g(x) - g(x_0)}{x - x_0} \cdot f(x) = \\ &= f'(x_0) \cdot g(x_0) + f(x_0) \cdot g'(x_0). \end{aligned}$$

So ,

$$\Phi'(x_0) = (f(x) \cdot g(x))'_{x_0} = f'(x_0) \cdot g(x_0) + f(x_0) \cdot g'(x_0) \blacktriangleright$$

3) $\frac{f(x)}{g(x)}$ function ($g(x_0) \neq 0$) x_0 at the point to the derivative have being _

$$\left(\frac{f(x)}{g(x)} \right)'_{x_0} = \frac{f'(x_0) \cdot g(x_0) - f(x_0) \cdot g'(x_0)}{g^2(x_0)}$$

will be

◀ As long as $g(x_0) \neq 0$ if , then x_0 of the point something around x in $g(x) \neq 0$ will be THAT attention take we find :

$$\begin{aligned} \frac{f(x) - f(x_0)}{g(x) - g(x_0)} &= \frac{f(x) \cdot g(x_0) - f(x_0) \cdot g(x_0) + f(x_0) \cdot g(x_0) - f(x_0) \cdot g(x)}{g(x) \cdot g(x_0) \cdot (x - x_0)} = \\ &= \frac{1}{g(x) \cdot g(x_0)} \left[\frac{f(x) - f(x_0)}{x - x_0} \cdot g(x_0) - f(x_0) \cdot \frac{g(x) - g(x_0)}{x - x_0} \right]. \end{aligned}$$

this equation $x \rightarrow x_0$ to the limit at past , this

$$\left(\frac{f(x)}{g(x)} \right)'_{x_0} = \frac{f'(x_0) \cdot g(x_0) - f(x_0) \cdot g'(x_0)}{g^2(x_0)}$$

to equality we will come $\blacktriangleright \left(\frac{2x - x^3}{\ln x} \right)'_{x=e}$ in derivative let's count . In this case, if $x=e$,

$$\left(\frac{2x - x^3}{\ln x} \right)'_{x=e} = \frac{(2x - x^3)' \ln x - (2x - x^3)(\ln x)'}{(\ln x)^2}$$

$(2x - x^3)' = 2 - 3x^2$ $(\ln x)' = \frac{x'}{x} = \frac{1}{x}$ so answer as follows harvest will be done .

$$\frac{(2 - 3x^2) \ln x - (2 - x^2)}{(\ln x)^2} \Big|_{x=e} = 2 - 3e^2 - 2 + e^2 = -2e^2$$

Result 1 . If $f(x)$ function x_0 at the point $f'(x_0)$ to the derivative have if _ _ $c \cdot f(x)$

function $(c = const)$ x_0 at the point to the derivative have be _ _ _

$$(c \cdot f(x))'_{x_0} = c \cdot f'(x_0)$$

will be , that is unchanging thig derivative from the hint out release can _

Result 2 . If $f_1(x), f_2(x), \dots, f_n(x)$ functions x_0 at the point to derivatives have being _ c_1, c_2, \dots, c_n unchanging numbers if , then

$$(c_1 f_1(x) + c_2 f_2(x) + \dots + c_n f_n(x))'_{x_0} = c_1 f_1'(x_0) + c_2 f_2'(x_0) + \dots + c_n f_n'(x_0)$$

will be

2^o . Complicated of the function derivative . Hypothesis let's do $y = f(x)$ function $X \subset R$ in $g(y)$ the collection function $\{f(x) | x \in X\}$ in the collection given being $x_0 \in X$ at the point $f'(x_0)$ to the derivative , $y_0 \in \{f(x) | x \in X\}$ at the point $(y_0 = f(x_0))$ $g'(y_0)$ to the derivative have let it be In that case $g(f(x))$ complicated function x_0 at the point to the derivative have being _

$$(g(f(x)))'_{x_0} = g'(f(x_0)) \cdot f'(x_0)$$

will be

◀ $g(y)$ of the function y_0 at the point $g'(y_0)$ to the derivative have because it was

$$g(y) - g(y_0) = g'(y_0) \cdot (y - y_0) + \alpha \cdot (y - y_0)$$

to be come it turns out that

$$y = f(x), y_0 = f(x_0) \text{ and } y \rightarrow y_0 \text{ at } \alpha \rightarrow 0$$

Next of equality each two side $x - x_0$ to being we find :

$$\frac{g(f(x)) - g(f(x_0))}{x - x_0} = g'(f(x_0)) \cdot \frac{f(x) - f(x_0)}{x - x_0} + \alpha \frac{f(x) - f(x_0)}{x - x_0}$$

From this $x \rightarrow x_0$ to the limit at passed _

$$(g(f(x)))'_{x_0} = g'(f(x_0)) \cdot f'(x_0)$$

to equality we will come ▶

30 . - The opposite of the function derivative . let's say $y = f(x)$ function (a, b) is given in , continuous and strictly increasing (constant decreasing) being $x_0 \in (a, b)$ at the point $f'(x_0)$ ($f'(x_0) \neq 0$) to the derivative have let it be In that case $x = f^{-1}(y)$ function $y_0 (y_0 = f(x_0))$ at the point to the derivative have and

$$[f^{-1}(y)]'_{x_0} = \frac{1}{f'(x_0)}$$

will be

◀ Ravshanka ,

$$f(x) - f(x_0) = f'(x_0)(x - x_0) + \alpha(x - x_0)$$

being and $x \rightarrow x_0$ $\alpha \rightarrow 0$ will be This from equality

$$y - y_0 = f'(x_0)[f^{-1}(y) - f^{-1}(y_0)] - \alpha[f^{-1}(y) - f^{-1}(y_0)] =$$

$$= [f^{-1}(y) - f^{-1}(y_0)] \cdot [f'(x_0) + \alpha]$$

to expression we will come From this while

$$\frac{f^{-1}(y) - f^{-1}(y_0)}{y - y_0} = \frac{1}{f'(x_0) + \alpha}$$

to be come comes out

Next in equality $y \rightarrow y_0$ to the limit at past we find :

$$[f^{-1}(y)]_{y_0} = \frac{1}{f'(x_0)} \cdot \blacktriangleright$$

4⁰. Examples . Example 1 . $(x^\alpha)' = \alpha x^{\alpha-1}$ will be , $\alpha \in R, x > 0$.

◀ Let's say $x > 0$ let it be In it $f(x) = x^\alpha$ function for

$$\frac{(x + \Delta x)^\alpha - x^\alpha}{\Delta x} = x^{\alpha-1} \cdot \frac{\left(1 + \frac{\Delta x}{x}\right)^\alpha - 1}{\frac{\Delta x}{x}}$$

being $\Delta x \rightarrow 0$ at $(x^\alpha)' = \alpha x^{\alpha-1}$ will be \blacktriangleright

Example 2 . $(a^x)' = a^x \ln a$ will be , $a > 0, x \in R$.

◀ $f(x) = a^x$ function for

$$\frac{a^{x+\Delta x} - a^x}{\Delta x} = a^x \cdot \frac{a^{\Delta x} - 1}{\Delta x}$$

being $\Delta x \rightarrow 0$ at $(a^x)' = a^x \ln a$ will be \blacktriangleright

Example 3 . $(\sin x)' = \cos x, (\cos x)' = -\sin x$ will be $x \in R$

◀ $f(x) = \sin x$ function for

$$\frac{\sin(x + \Delta x) - \sin x}{\Delta x} = 2 \cdot \frac{1}{\Delta x} \cdot \sin \frac{\Delta x}{2} \cos \left(x + \frac{\Delta x}{2}\right) = \frac{\sin \frac{\Delta x}{2}}{\frac{\Delta x}{2}} \cos \left(x + \frac{\Delta x}{2}\right)$$

being $\Delta x \rightarrow 0$ at $(\sin x)' = \cos x$ will be The same _ that's it similar $(\cos x)' = -\sin x$ to be found \blacktriangleright

Example 4 . $(\log_a x)' = \frac{1}{x \ln a}$ b dies , $a > 0, a \neq 1, x > 0$.

◀ $f(x) = \log_a x$ function for

$$\frac{\log_a(x + \Delta x) - \log_a(x)}{\Delta x} = \frac{1}{\Delta x} \log_a \left(1 + \frac{\Delta x}{x}\right) = \frac{1}{x} \log_a \left(1 + \frac{\Delta x}{x}\right)^{\frac{x}{\Delta x}}$$

being $\Delta x \rightarrow 0$ at

$$(\log_a x)' = \frac{1}{x} \log_a e = \frac{1}{x \ln a}$$

will be In particular, $(\ln x)' = \frac{1}{x}$ will be ►

Example 5. $(\arctg x)' = \frac{1}{1+x^2}$ will be

◀ Reverse function derivative count to the formula basically $(y = \arctg x, x = tgy)$

$$y' = (\arctg x)' = \frac{1}{(tgy)'} = \cos^2 y = \frac{1}{1+tg^2 y} = \frac{1}{1+x^2}$$

will be

Same that's it similar to

$$(\arcsin x)' = \frac{1}{\sqrt{1-x^2}} \quad (x \in (-1, 1)),$$

$$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}} \quad (x \in (-1, 1)),$$

$$(\text{arcctg} x)' = -\frac{1}{1+x^2}$$

will be .►

Example 6. Hypothesis let's do

$$y = [u(x)]^{v(x)} \quad (u(x) > 0)$$

being $u'(x)$ and $v'(x)$ are available let it be In that case

$$\left([u(x)]^{v(x)}\right)' = [u(x)]^{v(x)} \cdot \left[v'(x) \ln u(x) + \frac{v(x)}{u(x)} u'(x)\right]$$

will be _ _

◀ This $y = [u(x)]^{v(x)}$ n i logarithmically ,

$$\ln y = v(x) \ln u(x),$$

then we find the derivative of a complex function using the calculation rule:

$$\frac{1}{y} y' = v'(x) \cdot \ln u(x) + v(x) \cdot \frac{1}{u(x)} \cdot u'(x),$$

$$y' = y \left[v'(x) \cdot \ln u(x) + v(x) \cdot \frac{v(x)}{u(x)} \cdot u'(x) \right] =$$

$$= [u(x)]^{v(x)} \cdot \left[v'(x) \ln u(x) + \frac{v(x)}{u(x)} u'(x) \right]. \blacktriangleright$$

this,

$$(u^v)' = u^v \cdot \ln u \cdot v' + v \cdot u^{v-1} \cdot u'. \quad (3)$$

from equality , $y = u^v$ function derivative of calculation the following the rule come out :
 $y = u^v$ of the function derivative two from the joiner consists of being the first joiner u^v the indicative is taken as a function to the derivative (in which basis $u(x)$ is considered unchangeable) the second joiner while u^v the level is taken as a function to the derivative (in which degree indicator $v(x)$ is considered unchanged) is equal will be

Example 7 . This

$$f(x) = x^x, g(x) = x^{x^x}$$

of functions derivatives be found

◀ From formula (3). using we find :

$$f'(x) = (x^x)' = x^x \cdot \ln x + x \cdot x^{x-1} = x^x (\ln x + 1),$$

$$g'(x) = (x^{x^x})' = (x^{f(x)})' = x^{f(x)} \cdot \ln x \cdot f'(x) + f(x) \cdot x^{f(x)-1} =$$

$$= x^{x^x} \cdot \ln x \cdot (x^x (\ln x + 1)) + x^{x^x} \cdot x^{x^x-1} =$$

$$= x^{x^x+x-1} (x^x \ln x (\ln x + 1) + 1). \blacktriangleright$$

References

- 1.Leger G., Luks E. Generalized Derivations of Lie algebras, J. Algebra, 2000, 228,165-203.
- 2.Hartwig J., Larsson D.,Silvestrov S. Deformation of Lie algebras using (σ, τ) - derivation. Journal of algebra,2006, 38 (2) 109-138.
- 3.Hrivnak J.Invariants of Lie algebras. PhD Thesis, Faculty of Nuclear Science andPhysical Engineering, Czech Technical University, Prague, 2007.
- 4.Novotny P.,Hrivnak J. On (α, β, γ) -derivation of Lie algebras and corresponding invariant functions. J. Geom. Phys.,2008, 58, 208-217.
- 5.Rakhimov I. S., Said Husain Sh. K.,Abdulkadir A. On Generalized derivations of finite dimensional associative algebras. FEIC International journal of Engineering and Technology,2016, 13 (2) 121-126.
- 6.Fiidow M.A., Rakhimov I.S., Said Husain Sh.K., Basri W. (α, β, γ) -Derivations of diassociative algebras. Malaysian Journal Of Mathematical sciences, 2016, 10101- 126.
7. McCrimmon K.A taste of Jordan algebras.Springer, New York, Berlin, Heidelberg, Hong Kong, London, Milan, Paris, Tokyo, 2004, pp. 562.
8. Hanche-Olcen H., Störmer E.Jordan operator algebras.Boston etc: Pitman Publ. Inc.,1984, pp. 183.
9. Ergashev A. A., Vakhobov F. F. THE ESSENCE OF THE CONCEPT OF " PROFESSIONAL ACTIVITY OF A MATHEMATICS TEACHER" //Open Access Repository. – 2022. – T. 8. – №. 12. – C. 147-154.
- 10.Yigitalievich A. U., Fazliddin V. A SYSTEM OF EQUATIONS FOR OSCILLATION AND STABILITY OF A VISCOELASTIC PLATE TAKING INTO ACCOUNT THE GENERALIZED HEAT CONDUCTIVITY EQUATIONS “JOURNAL OF SCIENCE-INNOVATIVE RESEARCH IN UZBEKISTAN” JURNALI VOLUME 1, ISSUE 8, 2023. NOVEMBER ResearchBib Impact Factor: 8.654/2023 ISSN 2992-8869 337 //Galaxy International Interdisciplinary Research Journal. – 2022. – T. 10. – №. 12. – C. 304-308.

11. Makhmudov B. B., Vokhobov F. F. TOPICS: GAUSS'S THEOREM. INTEGRAL EXPRESSION OF THE HYPERGEOMETRIC FUNCTION ACCORDING TO THE DALANBER PRINCIPLE //Galaxy International Interdisciplinary Research Journal. – 2022. – T. 10. – №. 12. – C. 138-144.
12. Yigitalievich A. U., Mirsaid S. SYSTEM OF EQUATIONS OF COUPLED DYNAMIC PROBLEMS OF A VISCOELASTIC SHELL IN A TEMPERATURE FIELD //Galaxy International Interdisciplinary Research Journal. – 2022. – T. 10. – №. 12. – C. 298-303.
13. Faxriddinjon o'g'li V. F. et al. HYPERGEOMETRIC FUNCTIONS OF SEVERAL VARIABLES //Open Access Repository. – 2023. – T. 9. – №. 6. – C. 250-252.
14. Faxriddinjon o'g'li V. F. et al. EXPANSIONS OF HYPERGIOMETRIC FUNCTIONS OF SEVERAL VARIABLES ACCORDING TO KNOWN FORMULAS //Galaxy International Interdisciplinary Research Journal. – 2023. – T. 11. – №. 6. – C. 548-550.
15. Faxriddinjon o'g'li V. F. On Generalized Derivations Of Jordan Algebras //Open Access Repository. – 2022. – T. 9. – №. 11. – C. 340-343