

About the surface and its surface

K, DPI the author is F.F. Vokhobov

K, DPI the author is M.M. Sulaymanov

Abstract

This is it topic during curve line , his equations , curves of the line length , to length have didn't happen curve line about data is brought .

Key words . Surfaces, surfaces and to the surface have was forms in khaki

In the plain curve line this

$$\begin{cases} x = x(t), \\ y = y(t) \end{cases} \quad (\alpha \leq t \leq \beta)$$

equations system with (in particular , $y = f(x), (a \leq x \leq b)$ equation with) to be determined

we saw Ravshanki , crooked line $x(t), y(t)$ to functions depend _ If $x(t), y(t)$ functions $[\alpha, \beta]$

continuous at $x'(t), y'(t)$ to derivatives have if so , him smooth curve line it was called

Curved lines in theory important from concepts one curve of the line length is a curve to the line drawn broken line of fairy meter limit as defined and his length the following

$$l = \int_{\alpha}^{\beta} \sqrt{x'^2(t) + y'^2(t)} dt$$

with the formula expression in lectures statement done _

In the plain curve line to the concept similar in space surface concept when entered , his to himself special sides there is

In space simple surfaces - sphere, cylinder and that's it similar surfaces and their face _ _ count formulas to the student known .

We below common in appearance surfaces , their face , face to find formulas for the course need to be in volume briefly statement we will

1⁰ . Surface concept _ let's say UOV in the plain Δ in the collection

$$x = x(u, v), \quad y = y(u, v), \quad z = z(u, v) \quad (1)$$

functions given are , and they are Δ also continuous let it be $(u_0, v_0) \in \Delta$ point take , above functions at this point values we find :

$$x_0 = x(u_0, v_0), \quad y_0 = y(u_0, v_0), \quad z_0 = z(u_0, v_0).$$

Harvest has been (x_0, y_0, z_0) the R^3 in space M_0 of the point coordi natas that let 's see :

$M_0 = M(x_0, y_0, z_0)$ Ravshanki , (u, v) point Δ in the collection when it changes (x, y, z) s

R^3 in space something S the collection harvest does _ So , (1) relation Δ the collection S to the collection continuously reflection that to look can _

If (1) reflection mutually one valuable reflection if , that is Δ of the collection different

$(u, v), (\bar{u}, \bar{v})$ points S of the collection different $(x, y, z), (\bar{x}, \bar{y}, \bar{z})$ to the points reflects _ S the

collection R^3 in space surface that to look can _ Usually , it is surfaces simple surfaces is called

Because of this

$$\begin{cases} x = x(u, v), \\ y = y(u, v), \\ z = z(u, v) \end{cases} \quad ((u, v) \in \Delta) \quad (2)$$

equations system of the surface parametric equation he says , in this u and v s parameters .
Specifically ($u = x, v = y$ when) this

$$\begin{cases} x = x, \\ y = y, \\ z = f(x, y) \end{cases} \quad (3)$$

equations system which determines surface

equation with is expressed .

D_k collection T_k of orthogonal projection that it was for

$$\mu D_k = \mu T_k \cdot |\cos \gamma_k|$$

b dies in this $\gamma_k - S$ to the surface (ξ_k, η_k, z_k) ($z_k = f(\xi_k, \eta_k)$) nu q tada o' tka zil gan don't try
plain normal OZ bullet i with organize reached corner _

Ravshanki , $\lambda_{P_D} \rightarrow 0$ da $\lambda_{P_S} \rightarrow 0$ will be

If $\lambda_{P_D} \rightarrow 0$ at the following

$$\sum_{k=1}^n \mu T_k$$

now _ _ finite to the limit have if _ _ S surface surface have is called the value of the limit while
 S of the surface face is called S_0 ,

$$\mu S = \lim_{\lambda_{P_D} \rightarrow 0} \sum_{k=1}^n \mu T_k .$$

It is known that

$$\cos \gamma_k = \frac{1}{\sqrt{1 + f_x'^2(\xi_k, \eta_k) + f_y'^2(\xi_k, \eta_k)}}$$

being _

$$\mu T_k = \frac{1}{\cos \gamma_k} \cdot \mu D_k$$

from equality while

$$\sum_{k=1}^n \mu T_k = \sum_{k=1}^n \sqrt{1 + f_x'^2(\xi_k, \eta_k) + f_y'^2(\xi_k, \eta_k)} \cdot \mu D_k$$

b 's death come What is it ?

Next right of equality on the side now _ _

$$\sqrt{1 + f_x'^2(x, y) + f_y'^2(x, y)}$$

of the function integral sum will be This function D in the collection continuous , therefore integrable .

So ,

$$\lim_{\lambda_{P_D} \rightarrow 0} \sum_{k=1}^n \sqrt{1 + f_x'^2(\xi_k, \eta_k) + f_y'^2(\xi_k, \eta_k)} \cdot \mu D_k =$$

$$= \iint_D \sqrt{1 + f_x'^2(x, y) + f_y'^2(x, y)} dx dy.$$

So by doing S of the surface face

$$\mu S = \iint_D \sqrt{1 + f_x'^2(x, y) + f_y'^2(x, y)} dx dy \quad (4)$$

will be

Exercises

1. This $x^2 + y^2 + z^2 = R$ from the sphere the following $x^2 + y^2 = r^2 (r < R)$ of the cylinder cut received part of face be found

2. This $z = \frac{x^2}{2a} + \frac{y^2}{2b}$ elliptical of a paraboloid the following $\frac{x^2}{a^2} + \frac{y^2}{b^2} = c^2$ inside the cylinder is

located part of face be found

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