

## About the surface and its surface

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### Abstract

This is it topic during curve line , his equations , curves of the line length , to length have didn't happen curve line about data is brought .

**Key words** . Surfaces, surfaces and to the surface have was forms in khaki

In the plain curve line this

$$\begin{cases} x = x(t), \\ y = y(t) \end{cases} \quad (\alpha \leq t \leq \beta)$$

equations system with ( in particular ,  $y = f(x), (a \leq x \leq b)$  equation with ) to be determined we saw Ravshanki , crooked line  $x(t), y(t)$  to functions depend \_ If  $x(t), y(t)$  functions  $[\alpha, \beta]$  continuous at  $x'(t), y'(t)$  to derivatives have if so , him smooth curve line it was called Curved lines in theory important from concepts one curve of the line length is a curve to the line drawn broken line of fairy meter limit as defined and his length the following

$$l = \int_{\alpha}^{\beta} \sqrt{x'^2(t) + y'^2(t)} dt$$

with the formula expression in lectures statement done \_

In the plain curve line to the concept similar in space surface concept when entered , his to himself special sides there is

In space simple surfaces - sphere, cylinder and that's it similar surfaces and their face \_ \_ count formulas to the student known .

We below common in appearance surfaces , their face , face to find formulas for the course need to be in volume briefly statement we will

1<sup>0</sup> . Surface concept \_ let's say  $UOV$  in the plain  $\Delta$  in the collection

$$x = x(u, v), \quad y = y(u, v), \quad z = z(u, v) \quad (1)$$

functions given are , and they are  $\Delta$  also continuous let it be  $(u_0, v_0) \in \Delta$  point take , above functions at this point values we find :

$$x_0 = x(u_0, v_0), \quad y_0 = y(u_0, v_0), \quad z_0 = z(u_0, v_0).$$

Harvest has been  $(x_0, y_0, z_0)$  the  $R^3$  in space  $M_0$  of the point coordi natas that let 's see :

$M_0 = M(x_0, y_0, z_0)$  Ravshanki ,  $(u, v)$  point  $\Delta$  in the collection when it changes  $(x, y, z)$  s

$R^3$  in space something  $S$  the collection harvest does \_ So , (1) relation  $\Delta$  the collection  $S$  to the collection continuously reflection that to look can \_

If (1) reflection mutually one valuable reflection if , that is  $\Delta$  of the collection different

$(u, v), (\bar{u}, \bar{v})$  points  $S$  of the collection different  $(x, y, z), (\bar{x}, \bar{y}, \bar{z})$  to the points reflects \_  $S$

the collection  $R^3$  in space surface that to look can \_ Usually , it is surfaces simple surfaces is

called Because of this

$$\begin{cases} x = x(u, v), \\ y = y(u, v), \\ z = z(u, v) \end{cases} \quad ((u, v) \in \Delta) \quad (2)$$

equations system of the surface parametric equation he says , in this  $u$  and  $v$  s parameters . Specifically ( $u = x, v = y$  when ) this

$$\begin{cases} x = x, \\ y = y, \\ z = f(x, y) \end{cases}$$

equations system which determines surface

$$z = f(x, y) \quad (3)$$

equation with is expressed .

$D_k$  collection  $T_k$  of orthogonal projection that it was for

$$\mu D_k = \mu T_k \cdot |\cos \gamma_k|$$

b dies in this  $\gamma_k - S$  to the surface  $(\xi_k, \eta_k, z_k)$  ( $z_k = f(\xi_k, \eta_k)$ ) nu q tada o ' tka zil gan don't try plain normal  $OZ$  bullet i with organize reached corner \_

Ravshanki ,  $\lambda_{P_D} \rightarrow 0$  da  $\lambda_{P_S} \rightarrow 0$  will be

If  $\lambda_{P_D} \rightarrow 0$  at the following

$$\sum_{k=1}^n \mu T_k$$

now \_ \_ finite to the limit have if \_ \_  $S$  surface surface have is called the value of the limit while  $S$  of the surface face is called  $S_0$  ,

$$\mu S = \lim_{\lambda_{P_D} \rightarrow 0} \sum_{k=1}^n \mu T_k .$$

It is known that

$$\cos \gamma_k = \frac{1}{\sqrt{1 + f_x'^2(\xi_k, \eta_k) + f_y'^2(\xi_k, \eta_k)}}$$

being \_

$$\mu T_k = \frac{1}{\cos \gamma_k} \cdot \mu D_k$$

from equality while

$$\sum_{k=1}^n \mu T_k = \sum_{k=1}^n \sqrt{1 + f_x'^2(\xi_k, \eta_k) + f_y'^2(\xi_k, \eta_k)} \cdot \mu D_k$$

b 's death come What is it ?

Next right of equality on the side now \_ \_

$$\sqrt{1 + f_x'^2(x, y) + f_y'^2(x, y)}$$

of the function integral sum will be This function  $D$  in the collection continuous , therefore integrable .

So ,

$$\lim_{\lambda_{P_D} \rightarrow 0} \sum_{k=1}^n \sqrt{1 + f_x'^2(\xi_k, \eta_k) + f_y'^2(\xi_k, \eta_k)} \cdot \mu D_k =$$

$$= \iint_D \sqrt{1 + f_x'^2(x, y) + f_y'^2(x, y)} dx dy.$$

So by doing  $S$  of the surface face

$$\mu S = \iint_D \sqrt{1 + f_x'^2(x, y) + f_y'^2(x, y)} dx dy \quad (4)$$

will be

### Exercises

1. This  $x^2 + y^2 + z^2 = R$  from the sphere the following  $x^2 + y^2 = r^2 (r < R)$  of the cylinder cut received part of face be found

2. This  $z = \frac{x^2}{2a} + \frac{y^2}{2b}$  elliptical of a paraboloid the following  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = c^2$  inside the cylinder

is located part of face be found

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